

Appendix 1 to Wang S, Gong G, Zhong S, et al. Neurobiological commonalities and distinctions among three major psychiatric disorders: a graph theoretical analysis of the structural connectome. *J Psychiatry Neurosci* 2019.

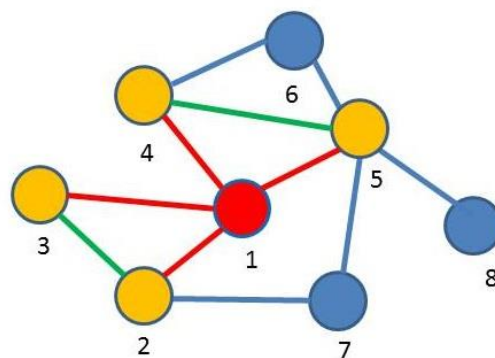
DOI: 10.1503/jpn.180162

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Supplementary materials

Figure S1. G_i and L_{ij}



G_i denotes the subgraph composed of the nearest neighbors of node i . For example, G_1 contains the nodes which have direction connections (the red edges in the paragraph) to node 1 and the connections between them (the red edges and the green edges).

G denotes the whole network.

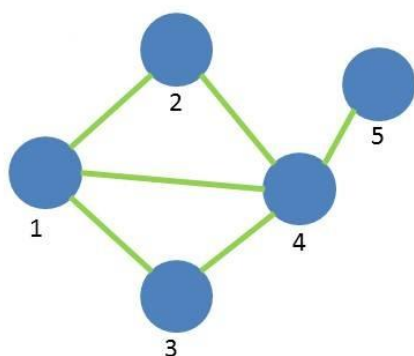
L_{ij} denotes the shortest path length between two node i and j , which is the smallest sum of the edges throughout all the possible paths in the graph from i to j , for example: $L_{13}=1$, $L_{18}=2$, $L_{38}=3\dots$

Figure S2. E_{glob}

Global Network Efficiency (E_{glob}) is described as the mean of the inverse of the shortest path length for all the nodes in the network. For a given network G with N nodes:

$$E_{glob}^G = \frac{1}{N(N-1)} \sum_{i \in G} \sum_{j \neq i \in G} \frac{1}{L_{ij}}$$

The E_{glob} reflects the capacity to facilitate parallel information transferring of the whole network.



For example, to calculate E_{glob}

$$L_{12} = 1, L_{13} = 1, L_{14} = 1, L_{15} = 2,$$

$$L_{23} = 2, L_{24} = 1, L_{25} = 2,$$

$$L_{34} = 1, L_{35} = 2$$

$$L_{45} = 1$$

$$L_{21} = 1, L_{31} = 1, L_{41} = 1, L_{51} = 2,$$

...

$$\begin{aligned} E_{glob} &= \frac{1}{N \times (N-1)} \times \left(\frac{1}{L_{12}} + \frac{1}{L_{13}} + \frac{1}{L_{14}} + \dots + \frac{1}{L_{54}} \right) \\ &= \frac{1}{5 \times (5-1)} \times \left(\frac{1}{1} + \frac{1}{1} + \frac{1}{1} + \dots + \frac{1}{1} \right) \\ &= 0.8 \end{aligned}$$

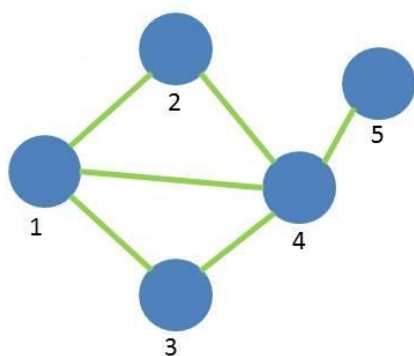
Figure S3. Eloc

The local efficiency of node i ($E_{loc}^{G_i}$) is defined as the global efficiency of G_i . The local efficiency of network (E_{loc}^G) is the mean of local efficiencies ($E_{loc}^{G_i}$) for all the nodes in the network, as below:

$$E_{loc}^G = \frac{1}{N} \sum_{i \in G} E_{loc}^{G_i}$$

N is the number of nodes of the network G

E_{loc}^G corresponds to the ability to tolerate faults of the whole network, i.e., if any node i in the network is destroyed, this ability can ensure the nodes of G_i still communicate information effectively with each other.



For example, to calculate E_{loc}^G

$$E_{loc}^{G_1} = \frac{1}{N^{G_1} \times (N^{G_1} - 1)} \times \left(\frac{1}{L_{23}} + \frac{1}{L_{24}} + \frac{1}{L_{32}} + \frac{1}{L_{34}} + \frac{1}{L_{42}} + \frac{1}{L_{43}} \right)$$

$$= \frac{1}{3 \times (3-1)} \times \left(\frac{1}{2} + \frac{1}{1} + \frac{1}{2} + \frac{1}{1} + \frac{1}{1} + \frac{1}{1} \right)$$

$$= \frac{5}{6}$$

$$E_{loc}^{G_2} = 1 \quad E_{loc}^{G_3} = 1 \quad E_{loc}^{G_4} = \frac{2}{3} \quad E_{loc}^{G_5} = 0$$

$$E_{loc}^G = \frac{1}{N} \times (E_{loc}^{G_1} + E_{loc}^{G_2} + E_{loc}^{G_3} + E_{loc}^{G_4} + E_{loc}^{G_5})$$

$$= \frac{1}{5} \times \left(\frac{5}{6} + 1 + 1 + \frac{2}{3} + 0 \right)$$

$$= 4.2$$

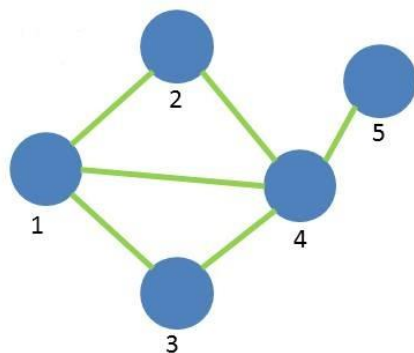
Figure S4. Enodal

The nodal efficiency (E_{nodal}) of a given node i is defined as the average inverse of the shortest path length between node i and all other nodes in the network, that is:

$$E_{\text{nodal}}^G(i) = \frac{1}{N-1} \sum_{i \neq j \in G} \frac{1}{L_{ij}}$$

N is the number of nodes of the network G

It represents the capacity of node i to communicate information with the other nodes in network.



For example, to calculate $E_{\text{nodal}}(1)$

$$L_{12} = 1$$

$$L_{13} = 1$$

$$L_{14} = 1$$

$$L_{15} = 2$$

$$\begin{aligned} E_{\text{nodal}}(1) &= \frac{1}{(N-1)} \times \left(\frac{1}{L_{12}} + \frac{1}{L_{13}} + \frac{1}{L_{14}} + \frac{1}{L_{15}} \right) \\ &= \frac{1}{(5-1)} \times \left(\frac{1}{1} + \frac{1}{1} + \frac{1}{1} + \frac{1}{2} \right) \\ &= 0.875 \end{aligned}$$